



## WORKSHOP 2009

Universidad Carlos III de Madrid  
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# Correlation between human activity and social connectivity in complex networks

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## SOCIAL NETWORKS

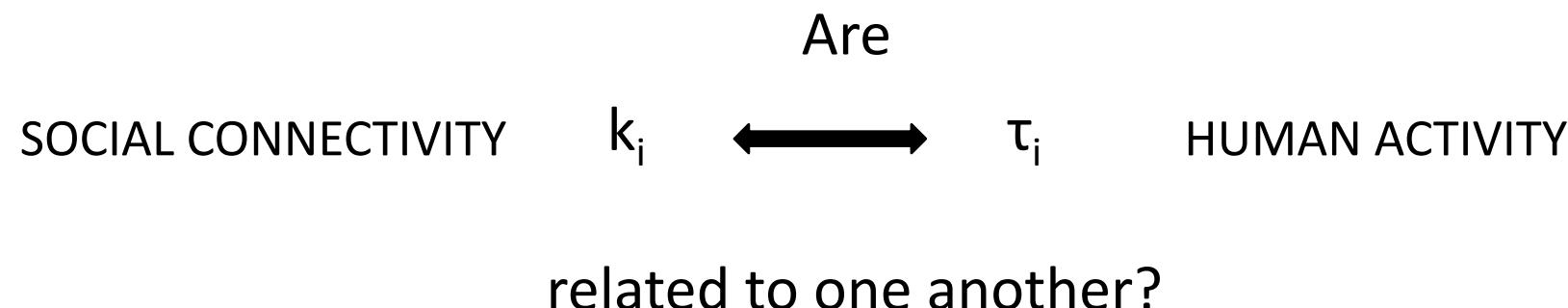
**WHAT PEOPLE HAVE STUDIED**

- ✓  $P(k)$  is scale-free  $P(k) \approx k^{-\gamma}$   
( i.e. networks of emails  $P(k) \approx k^{-2}$ )

**✓ MODELS**

- Preferential Attachment (Albert-Barabasi)
- Copying Mechanism (Kleinberg, Kumar et al)
- ...

- ✓  $P(k)$  influences the dynamics (i.e. percolation)

**WHAT WE WANT TO STUDY**

We studied the network of email traffic with email addresses as nodes and e-mails as links, using data from IBM server log files.

SENDER RECEIVER size TIME

1566	914	5430	6858423	3	1
2214	209	1262	6858428	3	1
1458	1077	1068	6858521	3	1
1566	1779	1458	6858621	3	1
1132	1727	492115	6858664	3	2
1132	1627	492115	6858664	3	2
4432	2675	2626	6858681	3	1
2063	2734	1025	6858685	3	1
1566	1758	1129	6858688	3	1
1772	1778	2818	6858699	3	1
1727	2855	9159	6858703	3	5
4432	2675	575	6858732	3	1
1727	223	9243	6858820	3	7
1727	284	9243	6858820	3	7
1566	1434	900	6858844	3	1
1132	1715	224092	6858860	3	2

Some statistical properties of the email network:

- total number of emails 202695

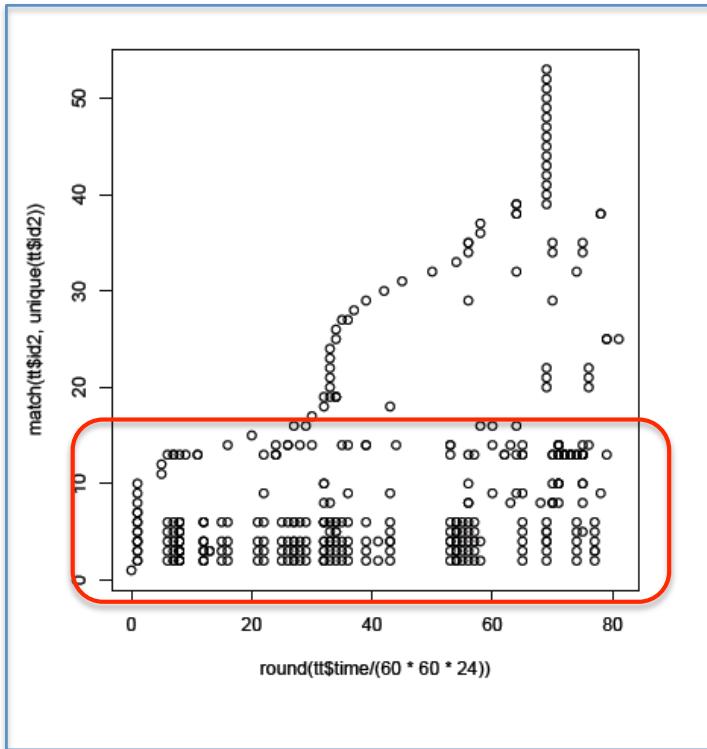
- number of vertices 2426

- total number of edges 14261

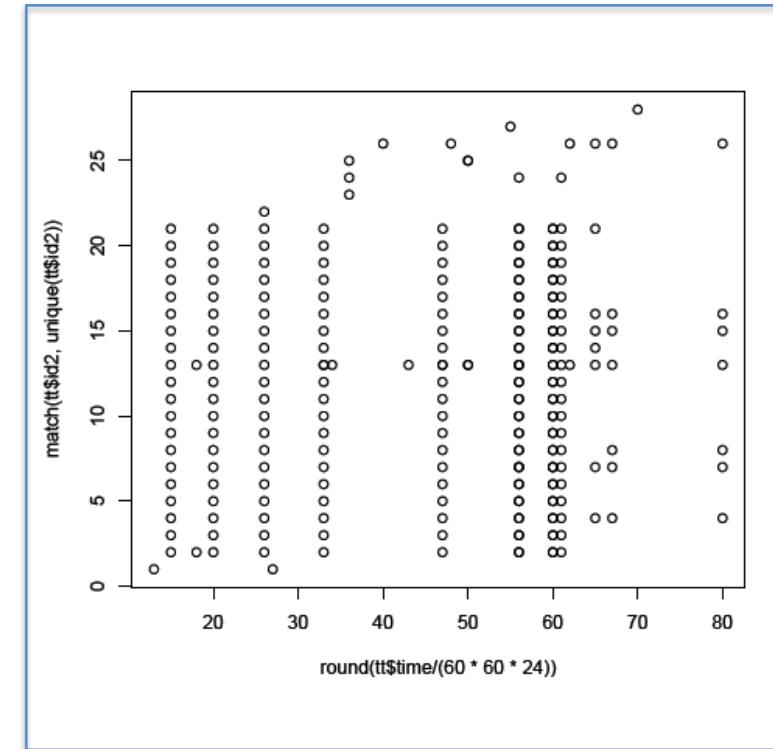
- time period under investigation  
 $T \approx 81$  days

## *Are they users or machines?*

Normal user



Machine-like user



We consider :

**dt** > 30 secs

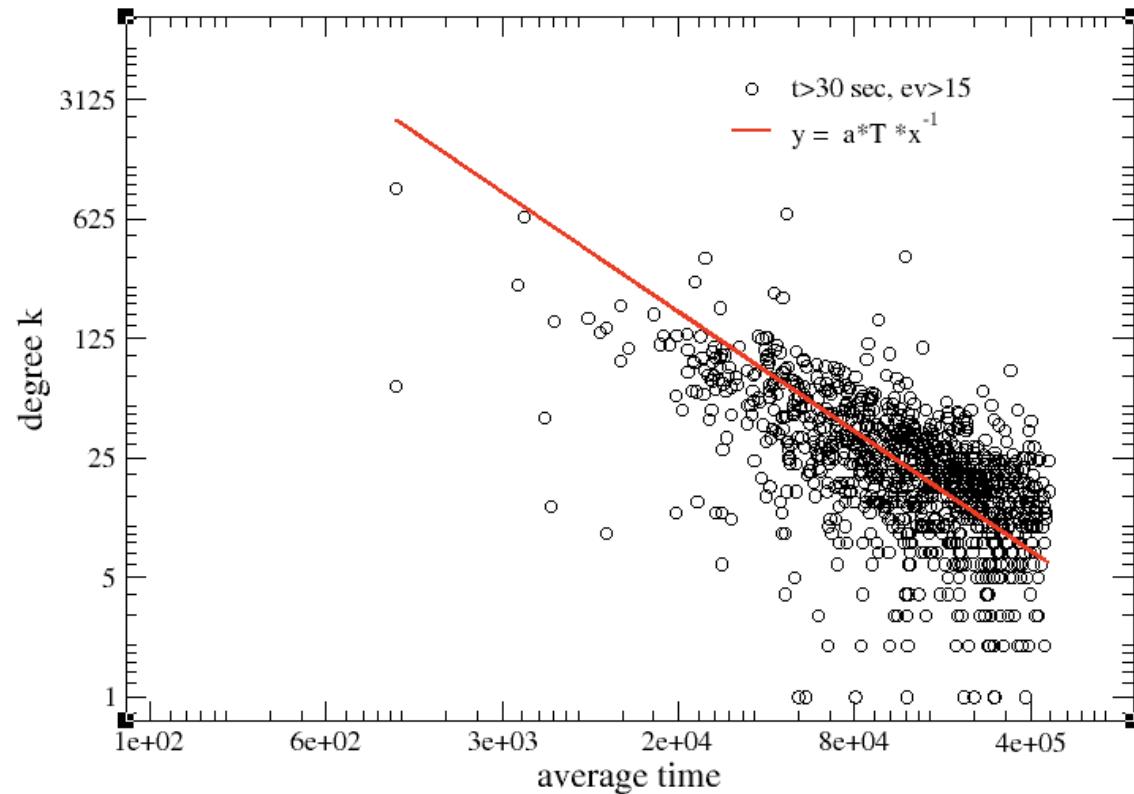
**events** (emails or groups of emails sent after a **dt** > 30 secs) > 15

This kind of user sends the same email to several contacts at the same time.  
..and sometimes they never write to them again.  
.. Are they actually “friends” ?

## RESULTS

$dt > 30$  secs

# events > 15



MODEL  
(red line)

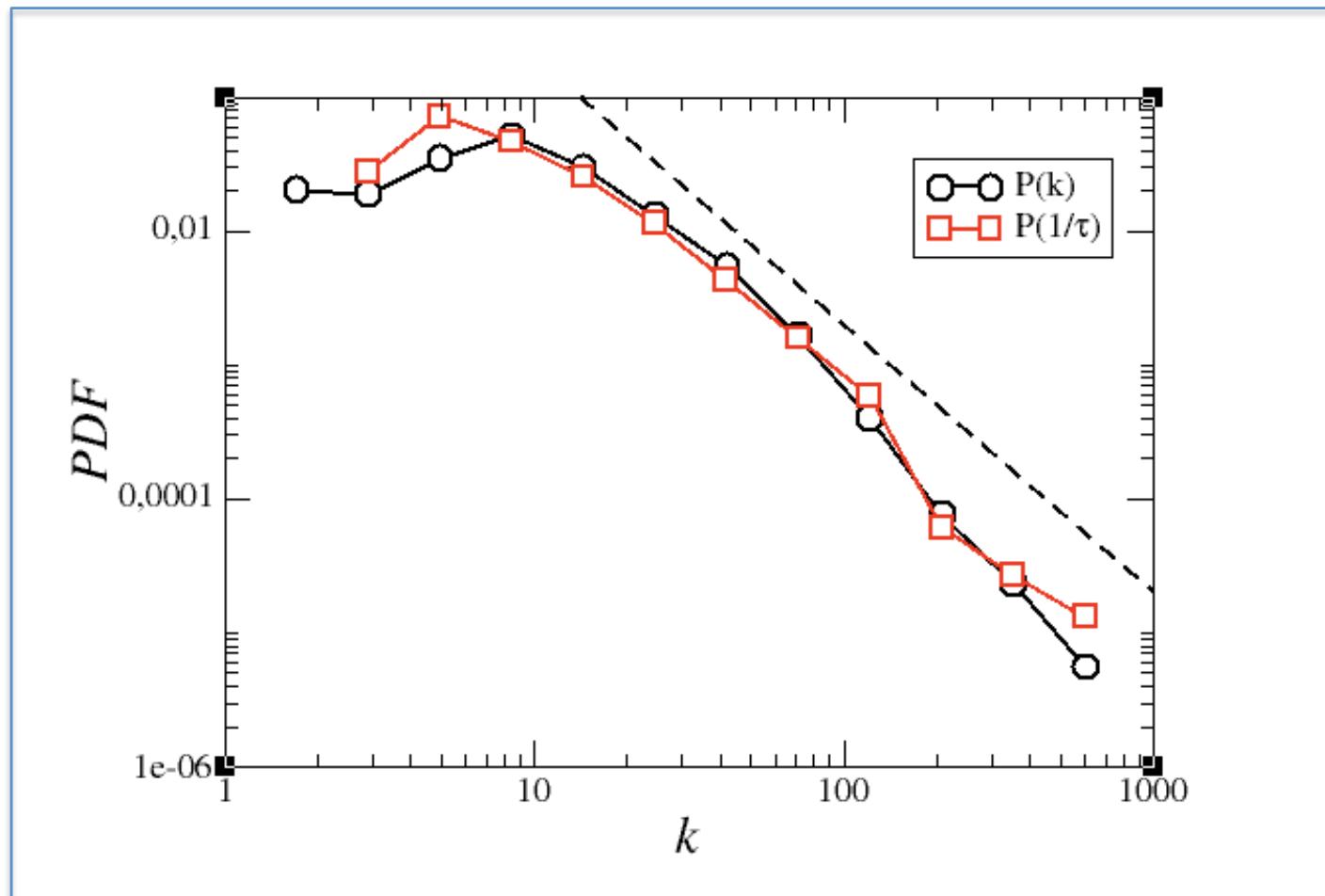
$$k_i \sim \alpha \frac{T}{\tau_i}$$

$k_i$  : degree  
 $\tau_i$  : average time

$$k_i \sim \alpha \frac{T}{\tau_i}$$



$$P_k(k) \sim -\frac{\alpha T}{k^2} P_\tau\left(\frac{\alpha T}{k}\right)$$



## CONCLUSIONS and PERSPECTIVES

- ☒ there is a relationship between  $k_i$  and  $\tau_i$  
$$k_i \sim \alpha \frac{T}{\tau_i}$$
- ☒  $P(k) \sim k^{-2}$  The exponent -2 does not come from any social dynamics
- ☒ Try to apply the method to some other (emails) networks