

EXCITONIC
AHARONOV-BOHM
EFFECT IN A
TWO-DIMENSIONAL
QUANTUM RING

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Workshop GISC 2012

SUMMARY

- Introduction
 - Excitonic Aharonov-Bohm effect
 - Experimental work
- Theoretical model
- Results
 - Exciton energy
 - Oscillator strength
 - Wavefunctions
- Conclusions

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Work done in collaboration with
Prof. Rudolf A. Römer

THE UNIVERSITY OF
WARWICK



Centre for Scientific Computing

INTRODUCTION

The Aharonov-Bohm effect

The Refractive Index in Electron Optics and the Principles of Dynamics

By W. EHRENBERG* AND R. E. SIDAY†

* Birkbeck College, University of London. † I.C.I. Fellow, Edinburgh University

*MS. received 23rd February 1948, and in amended form 28th July 1948;
read 3rd December 1948*

Proc. Phys. Soc. B 62 8 (1949)

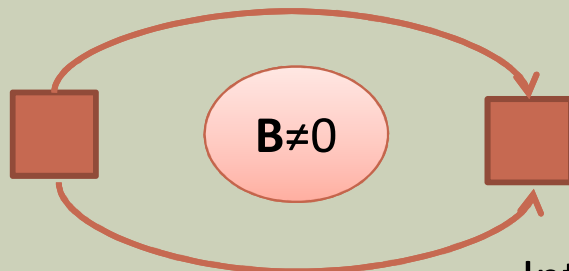
Significance of Electromagnetic Potentials in the Quantum Theory

Y. AHARONOV AND D. BOHM

H. H. Wills Physics Laboratory, University of Bristol, Bristol, England

(Received May 28, 1959; revised manuscript received June 16, 1959)

Physical Review 115, 485-491 (1959)



Electron source

Interference and
detection

$$\nabla \times \vec{A} = 0 = \vec{B}$$

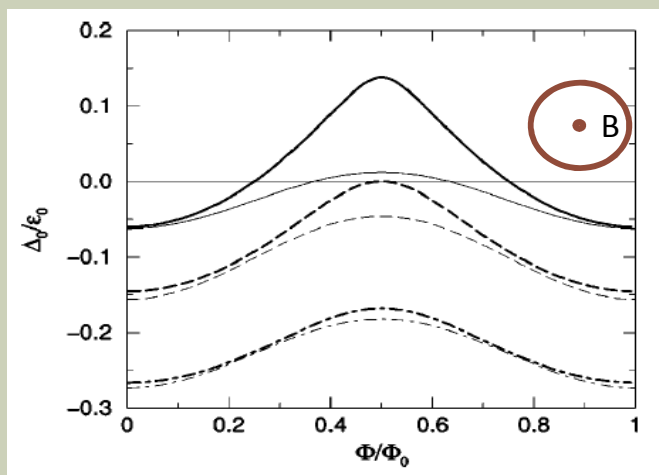
$$\oint d\vec{r} \vec{A} = \Phi$$

Phase difference $\Delta\alpha = 2\pi \frac{\Phi}{\Phi_0}$

$$\Phi_0 = h/e$$

INTRODUCTION

Excitonic Aharanov-Bohm effect



Exciton: neutral particle \rightarrow no sensitive to AB effect

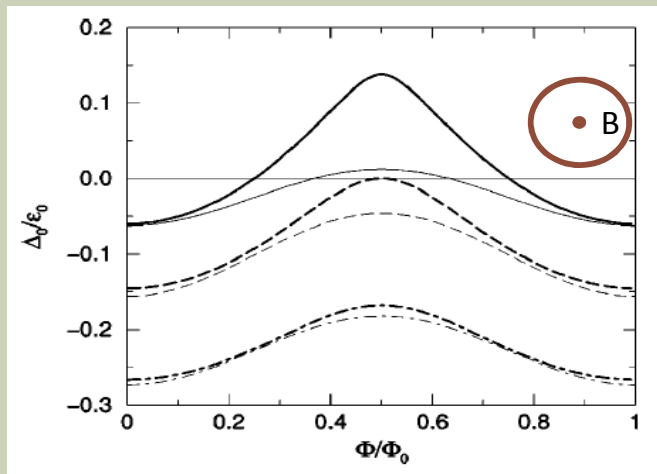
✓ Finite size and internal motion \rightarrow It is possible!

1D ring geometry +
perpendicular solenoid magnetic field +
contact electron-hole interaction

R. A. Römer and M. E. Raikh, PRB **62**, 7045 (2000)

INTRODUCTION

Excitonic Aharonov-Bohm effect



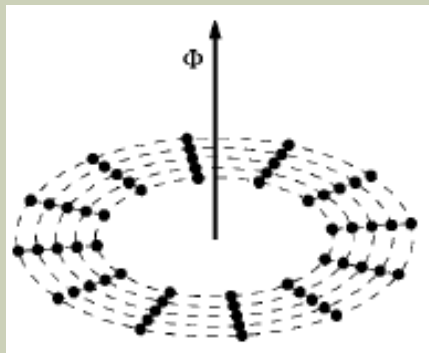
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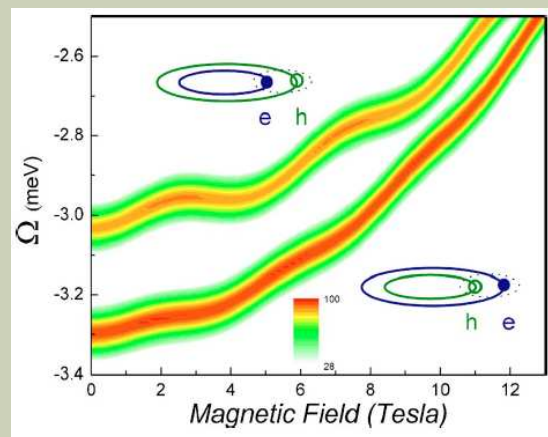
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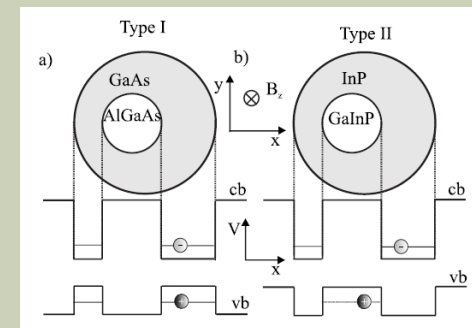
Other models:



PRB **63**, 125302 (2001)



PRB **72**, 125327 (2005)

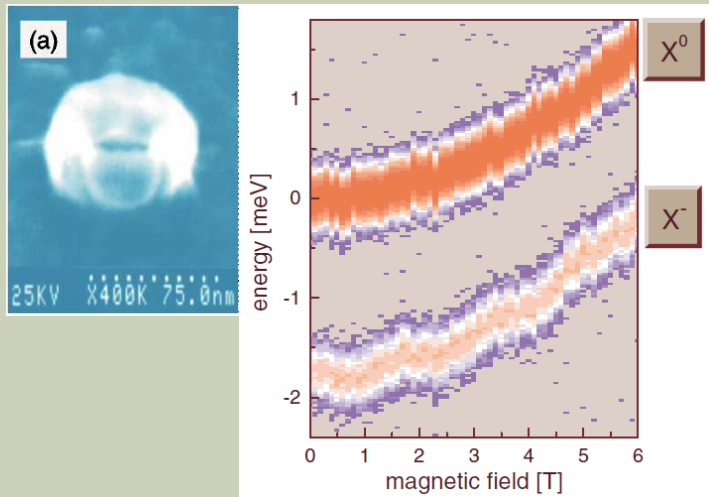


PRB **76**, 195326 (2007)

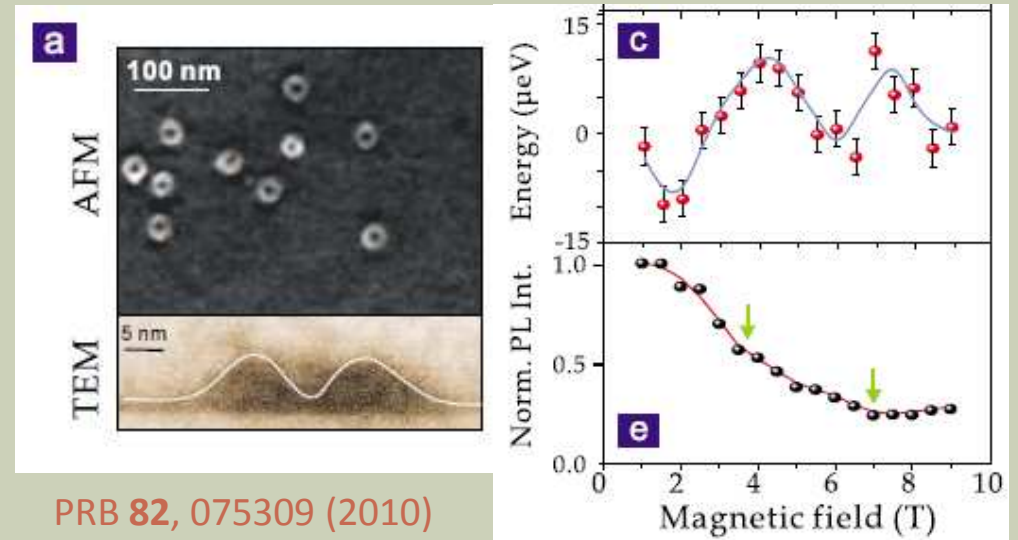
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INTRODUCTION

Experimental work

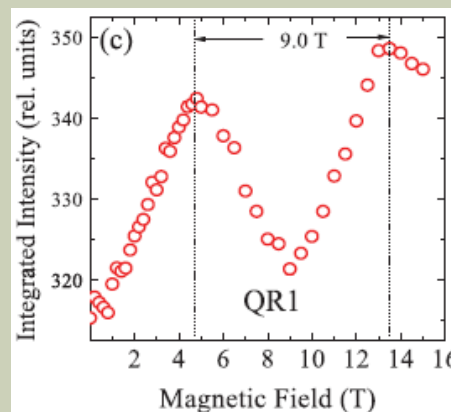
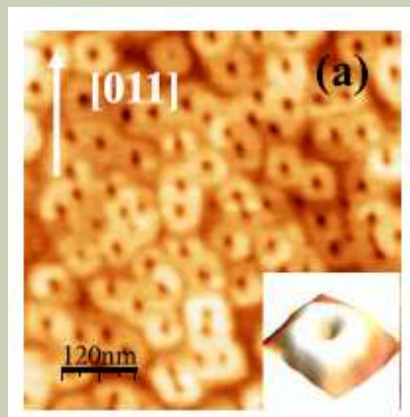


PRL **90**, 186801 (2003) Charged excitons



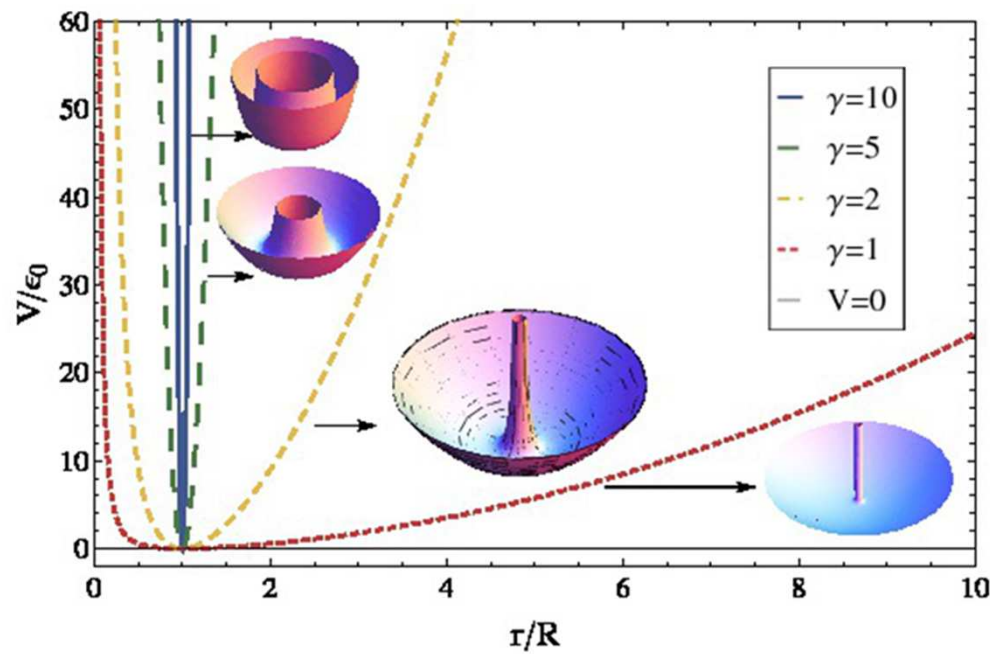
PRB **82**, 075309 (2010)

Molecular beam epitaxy of AsBr_3 in InGaAs QD



Self-assembled InAs/GaAs

PRL **104**, 086401 (2010)



$$V(r) = \frac{V_0}{2} \left[\frac{R^2}{r^2} + \frac{r^2}{R^2} \right] - V_0 \quad \gamma = R/W$$

Tan W.-C. and Inkson J. C., *Semicond. Sci. Technol.*, **11** 1635 (1996)

THEORETICAL MODEL

- Confining potential

Anharmonic, axially symmetric potential with a centrifugal core

$\gamma \rightarrow \infty$ 1D
 $\gamma \rightarrow 0$ anti-dot

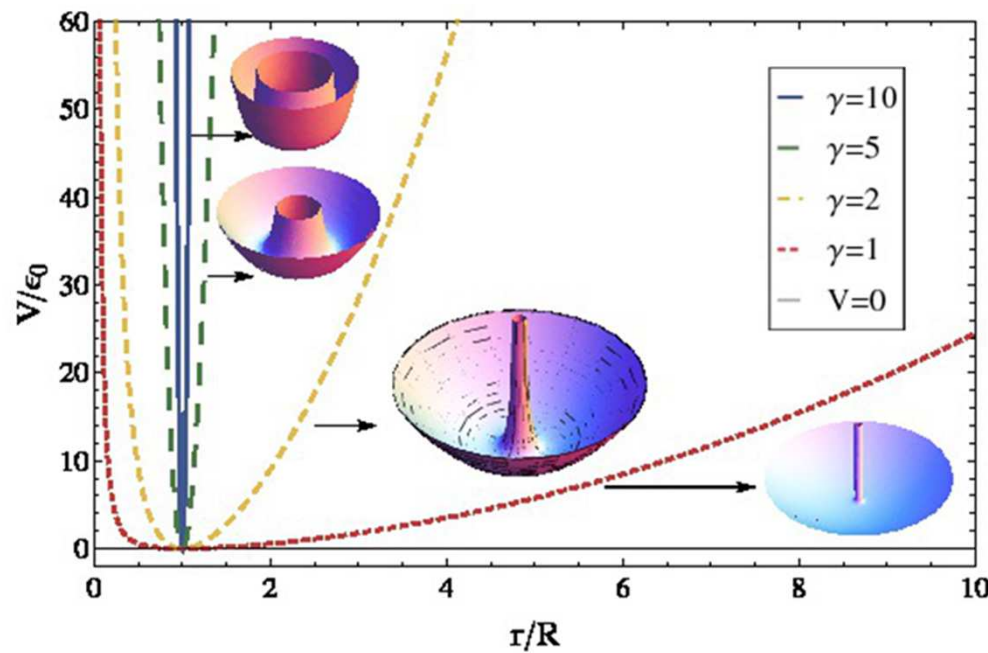
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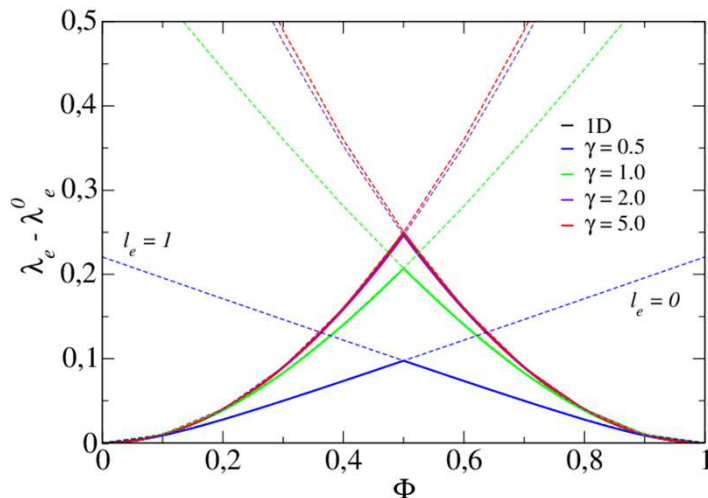
$\gamma \rightarrow \infty$ 1D
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- Single particle state in the QR



$$V(r) = \frac{V_0}{2} \left[\frac{R^2}{r^2} + \frac{r^2}{R^2} \right] - V_0 \quad \gamma = R/W$$

Tan W.-C. and Inkson J. C., Semicond. Sci. Technol., **11** 1635 (1996)



$$\psi_{M_e}(r_e) = \frac{e^{-il_e\theta_e}}{\sqrt{2\pi}} \mathcal{R}_{M_e}(r_e),$$

$$\mathcal{R}_{M_e}(r_e) = \frac{1}{R} \left[\frac{\Gamma(n_e + 1)}{2^{k_e} \Gamma(n_e + k_e + 1)} \right]^{1/2}$$

$$\times (\rho_e \gamma)^{k_e} e^{-\rho_e^2 \gamma^2 / 4} L_{n_e}^{k_e} \left(\frac{\rho_e^2 \gamma^2}{2} \right),$$

$$\mathcal{H}_{e-h}(\vec{r}_e, \vec{r}_h) = (2\pi)^{3/2} v_0 RW \delta(\vec{r}_e - \vec{r}_h)$$

$$v_0 = -\alpha/\pi^2$$

$$\Psi(\vec{r}_e, \vec{r}_h) = \sum_{M_e M_h} A_{M_e M_h} \psi_{M_e}(\vec{r}_e) \psi_{M_h}(\vec{r}_h)$$

$$G_{M_e' M_h'} = \sum_{M_e M_h} G_{M_e M_h} P_{M_e M_h M_e' M_h'}(\Delta)$$

$$G_{M_e M_h} = \int d^2 \vec{r} \Psi(\vec{r}, \vec{r}) \psi_{M_e}(\vec{r}_e)^\dagger \psi_{M_h}(\vec{r}_h)^\dagger$$

$$P_{M_e M_h M_e' M_h'} = -\frac{(2\pi)^{3/2} v_0 RW}{\lambda_{M_e} + \lambda_{M_h} - \Delta}$$

$$\times \underbrace{\int d^2 \vec{r} \psi_{M_e}(\vec{r}) \psi_{M_h}(\vec{r}) \psi_{M_e'}(\vec{r})^\dagger \psi_{M_h'}(\vec{r})^\dagger}_{\text{Reduces to an integral over the radial coordinates}}$$

$L = \ell_e + \ell_h = L' = 0$
Dipole approximation

Reduces to an integral
over the radial coordinates

THEORETICAL MODEL

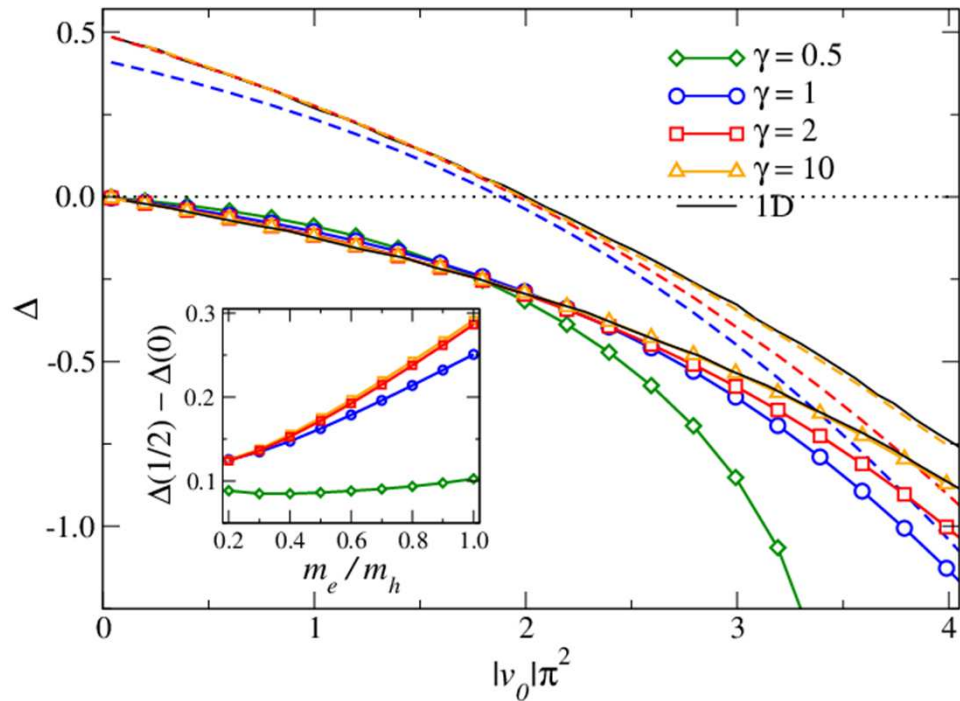
- Solution of the excitonic case

$$\mathcal{H} = \mathcal{H}_e + \mathcal{H}_h + \mathcal{H}_{e-h}$$

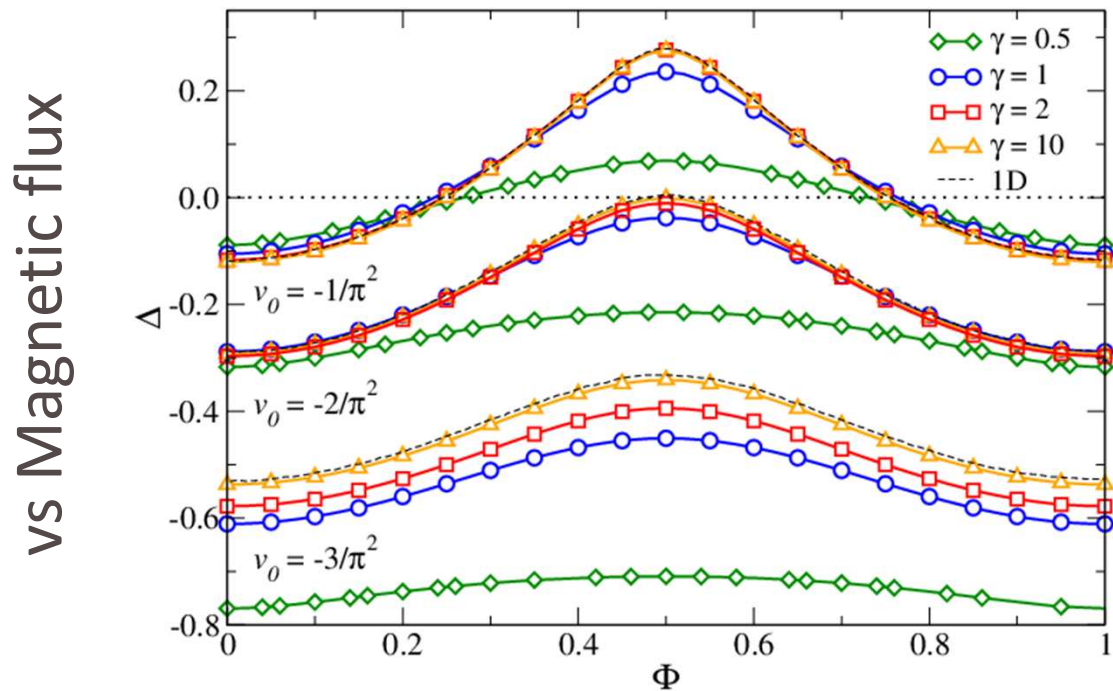
$$G_{K'} = \sum_K G_K P_{KK'}(\Delta)$$

Values of $\Delta \rightarrow$ eigenvalue
 $P_{KK'}$ equal to 1

Exciton ground state energy



vs Interaction strength

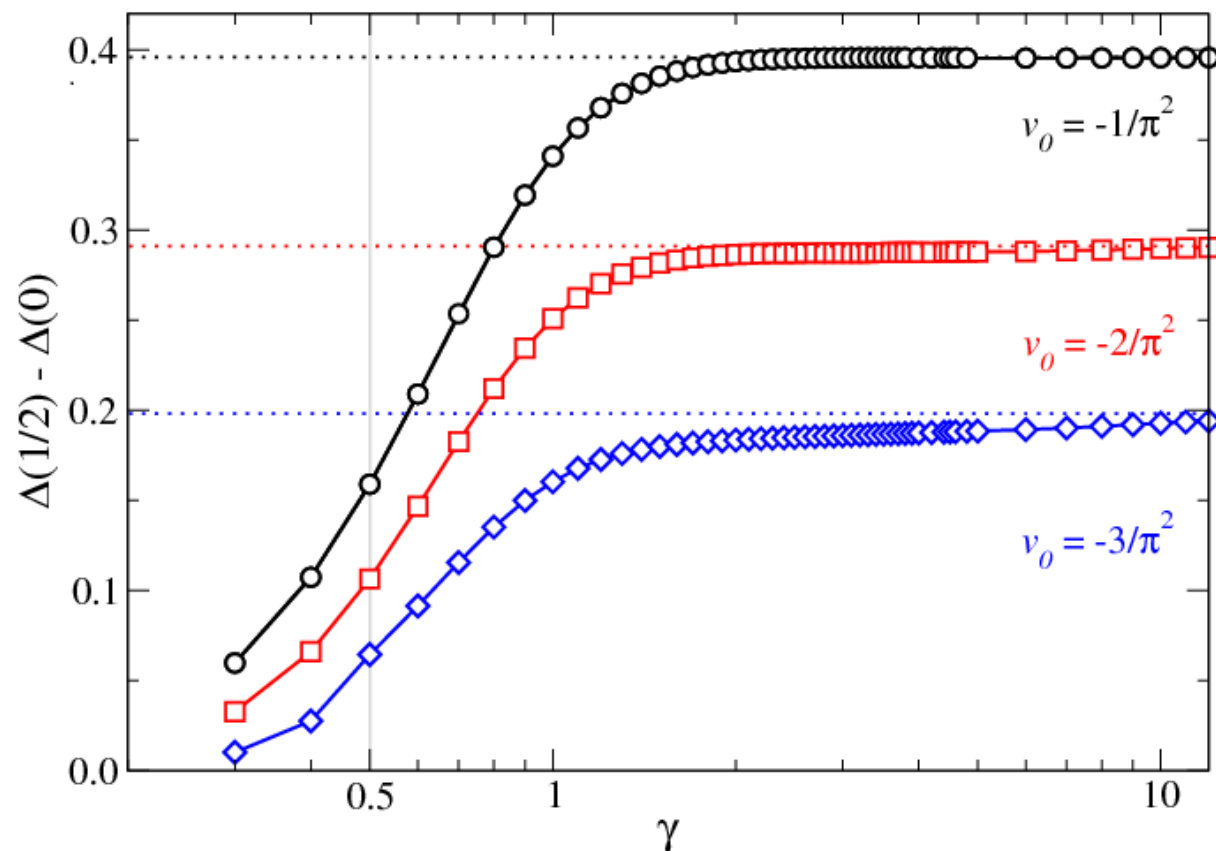


RESULTS

Excitons in 2D QR are also sensitive to magnetic flux

- For $\gamma = 10$:
2D behaviour similar to 1D
- AB oscillations retained from $\gamma=0.5$ to 10
- Different masses do not destroy the effect

Amplitude Aharonov-Bohm oscillations as a function of radius-to-width ratio

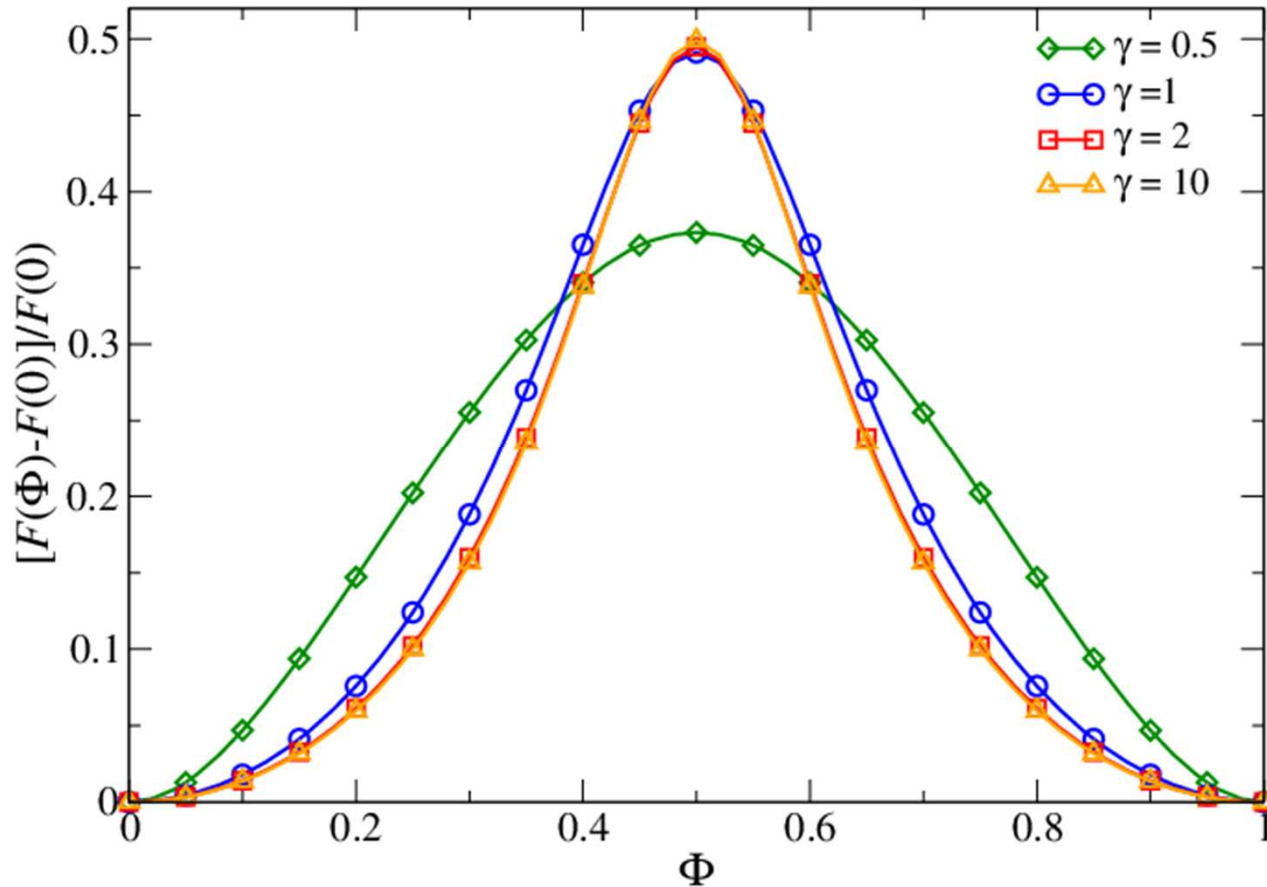


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- $\gamma = 0.5$ retains about 30-40% of the original AB amplitude (1D)

Oscillator strength



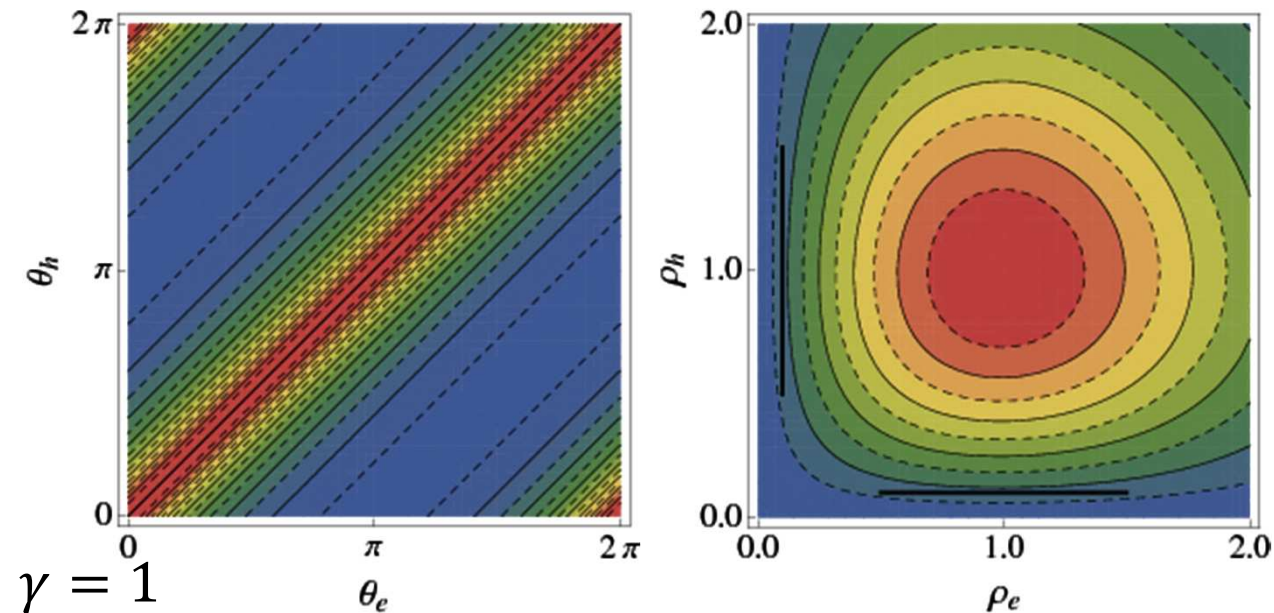
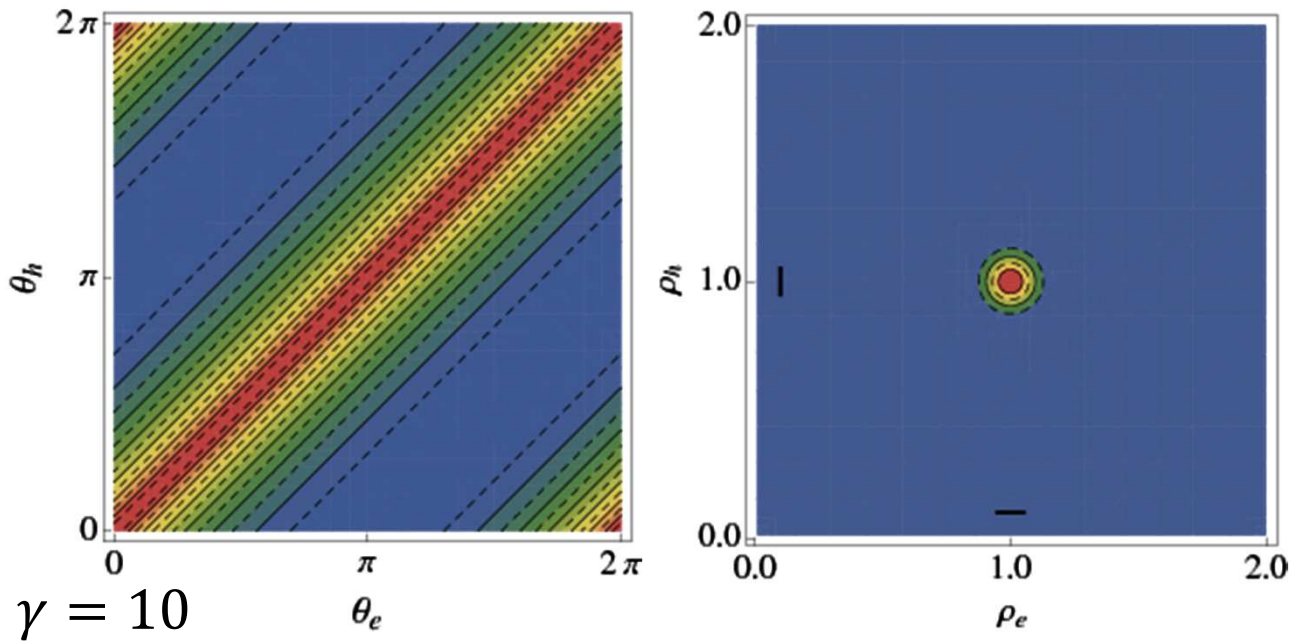
$$F = \frac{|\int d^2 \vec{r} \Psi(\vec{r}, \vec{r})|^2}{\int d^2 \vec{r}_e \int d^2 \vec{r}_h |\Psi(\vec{r}_e, \vec{r}_h)|^2}$$

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Local wavefunction probability



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- $F \neq 0 \rightarrow$ experimentally observable?
- Exciton fills QR width

CONCLUSIONS

- Excitonic AB predicted for 1D QR remains essentially unchanged in 2D
- When enlarge the ring width by one order of magnitude, the amplitude of the AB oscillations drops by about 15%
- Non-simply connected confined potential explains the presence of AB oscillations in 2D QR
- The behaviour of oscillations depends on the relative interaction strength to ring radius
- Our results are in good agreement with experimental results

Phys. Rev. B **84**, 235103 (2011)

¡MUCHAS GRACIAS!